

#### Outline

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- The assessment problem
- Modelling concepts and model selection
  - Why models?
  - Cohort analysis
  - Separable models
  - Time series analysis
- MSY explained
- Ecosystem considerations
- The catch-option table



Mean F





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## Concepts: Why models?



















$$B_{y+1} = B_y - M_y + R_y + G_y$$

#### **Concepts: Why models?**

- Model:
  - A way to simplify a system so we can understand it
- Trade off:
  - Complex / realistic v. simple / understandable
- Mathematics:
  - A language in which to write models down
- Model choice:
  - Available data
  - Purpose









• The total weight of mature fish in the stock

Abundance N x Weight Wt (kg) x Maturity Mat

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$$SSB = \sum_{a} N_{a} \times Wt_{a} \times Mat_{a}$$

#### **Concepts: Definitions**

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Recruitment R

- Abundance of fish entering the fishery
- Can depend on age (or size)
  - Cod large enough to be caught by age 1
  - Haddock appear in discards and bycatch by age 0 (towards the end of the year)
- Can also depend on location
  - Saithe usually stay in fjords until age 3 or 4



- F. I. Baranov (1918)
  - "On the Question of the Biological Basis of Fisheries", Nauchnye Issledovaniya Ikhtiologicheskii Instituta Izvestiya
- There are 100 fish, and 30 die
- Then the death rate is 30%
- Total mortality Z is just another way of writing death rate
  - Z is fishing mortality plus natural mortality





Total = Fishing

### **Concepts: The catch equation**

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• We can write the proportion of all deaths that are due to fishing:





F $\overline{Z}$ 

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• Suppose we also know the total number of fish:





#### **Concepts: The catch equation**

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• If we know the proportion P that die in a year, then the number of dead fish is:



 $P \times N$ 

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• Then the number that die due to fishing is:



#### **Concepts: The catch equation**

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• Which we just call the catch C:





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• IF we know catch and mortality, we can calculate abundance:

$$N = \frac{C}{\left(\frac{F}{Z}\right) \times P}$$

• But we can't easily estimate abundance and mortality at the same time!

Models: Cohort analysis





Models: Cohort analysis















Models: Cohort analysis





#### Models: Cohort analysis

- So if we know
  - Catch
  - Abundance
  - Natural mortality
- Then we can calculate fishing mortality
  - Except for the last year!
- But we **don't** know abundance...

### Concepts: Exponential decline

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• A cohort is assumed to decline exponentially:



#### **Concepts: Exponential decline**

- Key simplifying assumption:
  - Assume all catch taken at once
  - Pope's cohort approximation



#### Models: Cohort analysis

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- So we can do an assessment with catch data only
- Pros:
  - Many samples
- Cons
  - Fishermen follow fish
  - Some catch data may be missing
  - Difficult to estimate some Fs
- Survey data can help to address these problems

#### Models: Cohort analysis

- The key features of cohort analysis are:
  - Work backwards from last year
  - Add up catches
  - Add fish removed by natural mortality
  - "Tune" using surveys (if available)
  - Results in an estimate of the number of fish there must have been at the start of the cohort
- No statistical parameter estimation
  - Hence no estimates of uncertainty



### Models: Separable model

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- An analogy in fisheries is a **separable model** 
  - Two dimensional catch data (age and year)
  - Find a surface that passes as close to as many of the points as possible
  - Separable constraint:

$$Z_{a,y} = s_a \times f_y$$

- Enables uncertainty estimates



#### Models: Separable model

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- Example: SURBAR applied to NS lemon sole



# Concepts: The Kalman filter

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• Rudolf Kálmán (1960): modelling rocket trajectories



# Concepts: The Kalman filter



• Rudolf Kálmán (1960): modelling rocket trajectories





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• Example: SAM applied to North Sea cod



#### **Concepts: MSY**

- Maximum sustainable yield (MSY)
  - Assumes equilibrium (fishing mortality, growth etc. all unchanging)
  - Can be very uncertain
  - Can be difficult to fish all stocks at F(msy)
  - Different from maximum economic yield (MEY)





#### **Concepts: MSY**

- Maximum sustainable yield (MSY)
  - Used as the basis of ICES advice in the absence of management plans
  - Fishing at F(msy) can lead to stock reductions, so:
  - Calculation modified by risk considerations



#### The last stage: the catch-option table

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Rationale	Total catch 2017	Wanted catch 2017	Unwanted catch 2017	IBC 2017	Basis	Total F 2017	F(land) 2017	F(disc) 2017	F(IBC) 2017	SSB 2018	% SSB change	% TAC change
MSY	65.442	57.996	7.446	0.000	New F(msy) estimate	0.260	0.214	0.046	0.000	282	-23%	-10%
Mngmnt plan	74.372	65.895	8.477	0.000	MP target F	0.300	0.246	0.054	0.000	273	-25%	3%
IBC only	0.000	0.000	0.000	0.000	No HC fishery	0.000	0.000	0.000	0.000	343	-6%	-100%
Other options	56.150	49.771	6.379	0.000	0.75 * F(sq)	0.220	0.181	0.039	0.000	290	-20%	-22%
	72.785	64.491	8.294	0.000	Fsq	0.293	0.241	0.052	0.000	275	-24%	1%
	88.494	78.379	10.115	0.000	1.25 * F(sq)	0.366	0.301	0.065	0.000	260	-28%	22%
	64.311	56.995	7.316	0.000	15% TAC decrease (full)	0.255	0.209	0.046	0.000	283	-22%	-15%
	75.253	66.674	8.579	0.000	Rollover TAC (full)	0.304	0.250	0.054	0.000	273	-25%	0%
	85.739	75.945	9.795	0.000	15% TAC increase (full)	0.353	0.290	0.063	0.000	263	-28%	15%
	78.723	69.743	8.980	0.000	F(pa)	0.320	0.263	0.057	0.000	269	-26%	9%

Example: Northern Shelf haddock, October 2016

#### Summary

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### Thanks...

- Models make complex systems understandable
- Trade-off between simplicity and realism
- Many approaches to stock assessment exist
  - Often driven by data availability (but not always)
- The key end result (in ICES) is the catch-option table
  - Which is where managers take over!

